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# PERIOD ANALYSIS, ROCHE MODELING AND ABSOLUTE PARAMETERS FOR AU Ser, AN OVERCONTACT BINARY SYSTEM

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#### Abstract

CCD photometric data collected at UnderOak Observatory (UO) and Desert Bloom Observatory (DBO) in three bandpasses  $(B, V \text{ and } I_{\rm C})$  produced 10 new times of minimum for AU Ser which were used to revise the linear ephemeris. These results captured in 2011 and 2018 reinforced a longstanding observation that the shape of the light curve from this W UMa binary system (P=0.386497 d) is highly variable. Significantly skewed peaks and differences at maximum light were detected during quadrature which could only be simulated during Roche modeling by positioning a hot spot on the secondary star close to the neck between both constituents. Historically this system has been variously classified as an F8, G5 and K0 system; however, this study supports more recent reports that AU Ser is best described as spectral type K1V-K2V. A fresh assessment of eclipse time residuals over the past 80 years has provided additional insight regarding cyclical changes in orbital period experienced by this interesting variable star.

#### 1 Introduction

The W UMa variable AU Ser was first discovered by Hoffmeister (1935), visually observed by Soloviev (1951) and photographically recorded by Huth (1964). Since 1972, at least four different studies have produced photoelectrically-derived light curves (Binnendijk 1972; Kennedy 1985; Li et al. 1992; Li et al. 1998). CCD photometric (V-mag) data for this system were also captured by the All Sky Automated Survey (ASAS) between 2003 and 2009 (Pojmański 2005). Two spectroscopic investigations of this system (Hrivnak 1993; Pribulla et al. 2009) produced radial velocity (RV) results critical to determining a mass ratio ( $q = 0.71 \pm 0.02$ ) and total mass.

From the earliest studies it was obvious that AU Ser is subject to photospheric disturbances most likely resulting from either large cool spot(s) akin to sunspots or hot spot(s) potentially produced during mass transfer. Kałużny (1986) was the first to propose that the prominent light curve (LC) asymmetry observed during quadrature may be related to a hot spot located at the neck between both stars. Djurašević (1993) argued otherwise that based on a good fit to an RS CVn-based model (Djurašević 1992) for a detached system, there was no reasonable expectation for a hot spot to exist beyond the equatorial

zone of a star. Light curves generated by Li et al. (1998) further highlight the challenge in modeling this overcontact binary and even proposed the existence of short period oscillations at 0.0003 and 0.008 Hz. Period studies (Qian et al. 1999; Gürol 2005, Amin 2015 and Nelson et al. 2016) from eclipse timings that extend as far back as 1936 have revealed secular changes over the past 80 years. An underlying sinusoidal relationship in the eclipse timing differences (ETD) led the most recent three investigators to propose a third body orbiting the binary pair. Various opinions abound, but there is a general consensus that the secular decrease in eclipse timings most likely results from mass transfer and that the cyclic light-time-effect (LiTE) originates from the gravitational influence of an unseen third star. Herein we report on the analysis of new multicolor ( $BVI_{\rm C}$ ) LC data acquired in 2011 and 2018 along with a retrospective analysis of all evaluable LCs from AU Ser that are available from the literature. Furthermore, fresh LiTE analyses supported by the addition of 10 new eclipse timings has resulted in the refinement of a period solution for a putative gravitationally-bound third body.

# 2 Data

The imaging apparatus used during 2011 at UnderOak Observatory (UO; NJ, USA) included a 0.28-m Schmidt-Cassegrain telescope with an SBIG ST-8XME CCD camera mounted at the Cassegrain focus. Additional time-series photometric observations were acquired in 2018 at Desert Bloom Observatory (DBO: Benson, AZ, USA) with an SBIG STT-1603ME CCD camera mounted at the Cassegrain focus of a 0.4-m catadioptric telescope. In both cases photometric B, V and  $I_{\rm C}$  filters manufactured to match the Bessell prescription were used during each guided exposure (UO:75 s and DBO:60 s). Specifics regarding image acquisition, calibration, registration and reduction to catalog-based magnitudes (MPO Canopus) have been reported elsewhere for UO (Alton 2016) and DBO (Alton 2018). Roche type modeling was performed with the assistance of Binary Maker 3 (BM3; Bradstreet and Steelman 2002), WDwint56a (Nelson 2009), and PHOEBE 0.31a (Prša and Zwitter 2005), the latter two of which employ the Wilson-Devinney (W-D) code (Wilson and Devinney 1971; Wilson 1979; Wilson 1990). Spatial renderings of AU Ser were also produced by BM3 once model fits were finalized. Times-of-minimum were calculated using the method of Kwee and van Woerden (1956).

### 3 Results

#### 3.1 Photometry and Ephemerides

An ensemble of five stars in the same field-of-view with AU Ser (Fig. 1) was used to ultimately derive catalog-based magnitudes (Table 1). These stars exhibited no evidence of inherent variability (V and  $I_{\rm C} < 0.03$  mag and B < 0.05 mag) beyond experimental error over each imaging session. Photometric data in B (n=270), V (n=276), and  $I_{\rm C}$  (n=284) were processed to generate bandpass specific LCs collected between 11 July 2011 and 22 July 2011 (Figs. 2 & 3). Additional photometric data acquired during a recent photometric campaign (29 May - 11 June 2018) in B (n=372), V (n=372) and  $I_{\rm C}$  (n=374), were similarly folded by Fourier analysis (Figs. 2 & 3).

In total, six new secondary (s) and four primary (p) minima were captured during this investigation which also included a single isolated session on 25 June 2015 at UO. All times-of-minima were averaged (Table 2) from each session since the chronological order of eclipse timings (ET) showed no color dependency. The Fourier routine (FALC;

<b>Table 1.</b> FOV identity, name, astrometric coordinates and color index $(B-V)$ for the target
(AU Ser=T) and comparison stars (1-5) used for ensemble aperture photometry

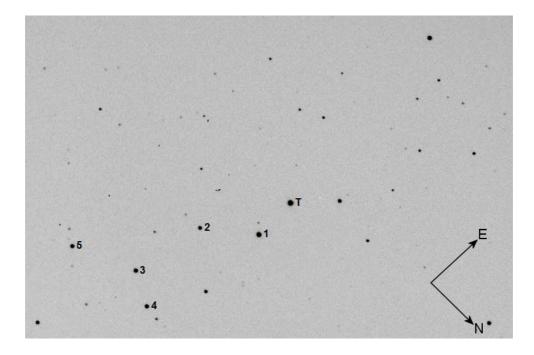
FOV	Name	$\alpha_{2000.0}$	$\delta_{2000.0}$	MPOSC3 <sup>a</sup>
Identity		hh mm ss	0 / //	(B-V)
1	TYC 01502-1573-1	15 56 43.12	$+22\ 16\ 01.6$	0.685
2	GSC $01502-1653$	$15\ 56\ 35.24$	$+22\ 15\ 35.3$	0.577
3	GSC $01502-1352$	$15\ 56\ 23.66$	$+22\ 16\ 06.6$	1.070
4	TYC 01502-1613-1	$15\ 56\ 23.12$	$+22\ 17\ 25.9$	1.153
5	GSC 01502-1418	$15\ 56\ 16.13$	$+22\ 14\ 27.6$	0.621
${ m T}$	AU Ser	$15\ 56\ 49.47$	$+22\ 16\ 01.6$	0.834

a: MPOSC3 is a hybrid catalog which includes a large subset of the Carlsberg Meridian Catalog (CMC-14) as well as from the Sloan Digital Sky Survey (Warner 2007).

Harris 1989) in MPO Canopus (2015) provided an identical period solution (0.386497  $\pm$  0.000001d) for the multicolor data captured in 2011 and 2018. An updated linear ephemeris equation (1) based on the linear elements defined by Kreiner (2004) was calculated using the last 7 years (Table 2) of published ET data:

$$Min I(Hel.) = 2458280.7899(14) + 0.3864965(1) E.$$
 (1)

Given the complex changes in orbital period observed for this system (see Section 3.6), new eclipse timings for AU Ser should be determined on a regular basis to maintain an accurate record about the behavior of this variable system.



**Figure 1.** Observed field-of-view (FOV) for AU Ser (T=target) obtained at DBO. The comparison stars are marked according to the numbers (1-5) assigned in Table 1.

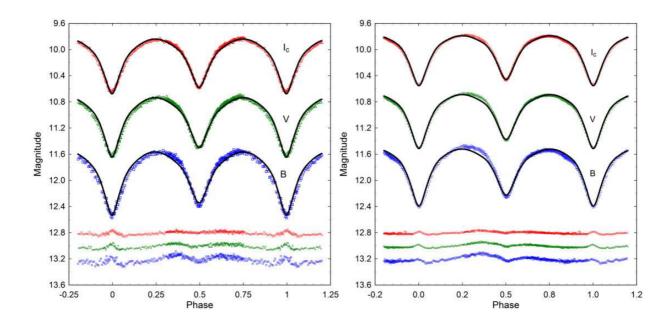


Figure 2. Folded ( $P=0.386497\pm0.000001$  d) light curves ( $BVI_{\rm C}$ -mag) for AU Ser produced from data collected in 2011 at UO (left) and during 2018 at DBO (right). Roche model fits using the W-D code were determined without the addition of a spot. For presentation convenience, the corresponding residuals shown at the bottom are offset from zero.

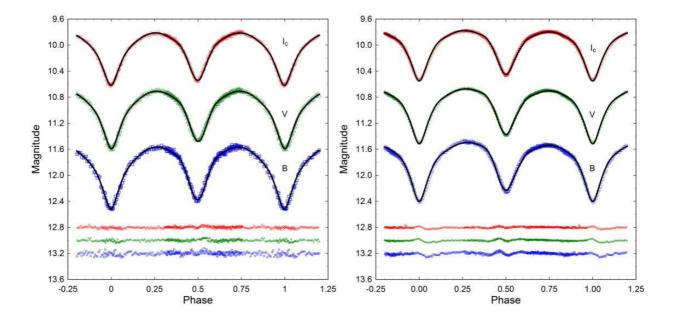


Figure 3. Folded ( $P = 0.386497 \pm 0.000001$  d) light curves ( $BVI_{\rm C}$  mag) for AU Ser produced from data collected in 2011 at UO (left) and during 2018 at DBO (right). Roche model fits using the W-D code were determined with the addition of a single hot spot in the neck region of the secondary star. For presentation convenience, the corresponding residuals shown at the bottom are offset from zero.

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**Table 2.** Eclipse time differences (ETD) between 2011 and 2018 calculated from published times of minima (ToM) for AU Ser along with ten new values reported for the first time in this study

HJD (ToM)	Cycle	ETD	Minimum	Reference
-2400000	Number		Type	
55753.6815 (1) <sup>a</sup>	8417.5	-0.00055	S	This study
55756.5814 (14)	8425	0.00059	p	This study
55760.6388(1)	8435.5	-0.00021	$\mathbf{s}$	This study
55764.6971(3)	8446	-0.00010	p	This study
56034.8573(1)	9145	-0.00175	p	1
56065.3904(4)	9224	-0.00196	p	2
56511.4074(2)	10378	-0.00318	p	3
56782.5374(9)	11079.5	-0.00126	$\mathbf{s}$	4
56783.5018(7)	11082	-0.00310	p	4
56787.3675(1)	11092	-0.00238	p	5
56787.3678(1)	11092	-0.00207	p	6
56812.4894(9)	11157	-0.00282	p	4
57084.9700(1)	11862	-0.00303	p	7
$57108.1609  (^{\rm b})$	11922	-0.00199	p	8
57135.7953(3)	11993.5	-0.00217	$\mathbf{s}$	7
57136.5691 (20)	11995.5	-0.00136	$\mathbf{s}$	9
57198.6010(2)	12156	-0.00237	p	This study
57246.3338(1)	12279.5	-0.00198	$\mathbf{s}$	5
57414.6499(3)	12715	-0.00555	p	10
57480.5515(7)	12885.5	-0.00182	$\mathbf{s}$	5
57514.3682(16)	12973	-0.00366	p	9
57514.5613(8)	12973.5	-0.00381	$\mathbf{s}$	9
57515.5275(8)	12976	-0.00386	p	9
58257.7919(2)	14896.5	-0.00810	$\mathbf{s}$	This study
58267.8408(1)	14922.5	-0.00817	$\mathbf{s}$	This study
58274.7979(1)	14940.5	-0.00804	$\mathbf{s}$	This study
58276.7312 (1)	14945.5	-0.00720	$\mathbf{s}$	This study
58280.7886(1)	14956	-0.00802	p	This study

a: Throughout this paper tabulated uncertainty in least significant figure(s) provided within adjacent parentheses.

b: not reported;

<sup>1.</sup> Diethelm 2012; 2. Hübscher & Lehmann 2013 3. Hoňková et al. 2014; 4. Hübscher & Lehmann 2015;

<sup>5.</sup> Parimucha et al. 2016; 6. Hoňková et al. 2015; 7. Nelson 2016; 8. Nagai 2016; 9. Hübscher 2017;

<sup>10.</sup> Juryšek et al. 2017

#### 3.2 Light Curve Behavior from 2011 and 2018

As is typical for overcontact binary systems, light curves from AU Ser (Figs. 2 & 3) exhibit minima which are separated by 0.5 phase ( $\phi$ ) and consistent with synchronous rotation in a circular orbit. Maximum light during the 2011 campaign was nearly equal (Max I  $\sim$  Max II) within each bandpass; however, there is significant displacement whereby the brightest values occur after  $\phi = 0.25$  (+0.03) and before  $\phi = 0.75$  (-0.03). This effect is most obvious in B band and results in skewed peaks during quadrature. Similar behavior is observed with the 2018 light curves (Figs. 2 & 3), except that during this epoch Max I is notably brighter than Max II. It would appear that some kind of surface phenomenon distorts maximum light. Data from folded 2011 LCs B, V and  $I_{\rm C}$  mag) were binned into equal phase intervals (0.002) to produce plots in which color index changes in B - V (Fig. 4: left) and  $V - I_{\rm C}$  (Fig. 4: right) were examined during each orbital phase. Deviation is quite remarkable suggesting that the localized effective temperature increased considerably during quadrature when the neck is maximally exposed.

Surface inhomogeneities have been associated with the presence of cool starspot(s), hot region(s), gas stream impact on either stellar partner, and/or other unknown mechanisms (Yakut and Eggleton 2005). As will be described in more detail in Section 3.4, positioning a hot spot on or near the neck region of the secondary star provided much improved Roche model solutions for the light curve asymmetry observed from 1969-2018. As mentioned earlier, Kałużny (1986) first proposed that a hot spot was responsible for the pronounced asymmetry observed in light curves captured in 1969 and 1970 by Binnendjik (1972). This is in contrast to Roche modeling (W-D) performed by Gürol (2005) who concluded these LCs along with those collected in 1995 (Li et al. 1998) and 2003 (Gürol 2005) were best fit with cool spots on the secondary. Gürol (2005) did, however, show that simulated light curves collected in 1991 (Li et al. 1998) and 1992 (Li et al. 1998) benefited from hot spots on the secondary albeit not in the neck region. It should also be mentioned that Gürol (2005) took an unorthodox approach by allowing  $A_2$ , the reflection-coefficient of the secondary, to freely vary during model optimization by differential corrections (DC). As a result the derived values were much larger (3.25–4.44) than the bolometric albedo value (0.5) usually assigned to systems with a convective envelope.

#### 3.3 Effective Temperature

Color index (B-V) data from UO and five other surveys (Table 3) were corrected using the interstellar extinction ( $A_V = 0.065$ ; E(B-V) = 0.021 assuming R = 3.1) estimated for targets within the Milky Way Galaxy according to Amôres and Lépine (2005). The interstellar extinction model GALExtin<sup>1</sup> requires the Galactic coordinates (l, b) and the estimated distance in kpc. In this case the value for  $A_V$  (0.065) corresponds to a target located within 164 pc (see Section 3.5). By contrast the dust maps constructed by Schlegel et al. (1998) and updated by Schlafly and Finkbeiner (2011) determine extinction ( $A_V = 0.172$ ) based on total dust infrared emission in any given direction and not the extinction within a certain distance. In many cases the net effect for relatively close (<1 kpc) stellar objects within the Milky Way Galaxy is an overestimation of reddening. The mean result for intrinsic color,  $(B-V)_0 = 0.859 \pm 0.021$ , which was adopted for subsequent Roche modeling corresponds to an effective temperature of 5140 K (Pecaut and Mamajek 2013) and ranges in spectral class between K1V and K2V. The  $(V-I_C)_0$  color index estimate  $(0.91\pm0.02)$  for the primary star taken at Min II when the secondary nearly reaches total

<sup>1</sup>http://www.galextin.org/v1p0/

<b>Table 3.</b> Effective temperature of AU Ser based upon dereddened $(B-V)^a$	
data from various surveys and the present study	

Stellar Attribute	Terrell et al. (2012)	2MASS	SDSS-DR8	UCAC4	$ASCC^d$	This Study
$(B-V)_0$	0.867	0.820	0.878	0.882	0.806	0.851
$T_{\rm eff}^{\rm b} ({ m K})$	5113	5267	5082	5071	5295	5158
Spectral Class <sup>b</sup>	K1-K2V	K0-K1V	K1- $K2V$	K1V-K2V	G9V-K0V	K1-K2V

a: E(B-V) = 0.021

eclipse is also consistent with a K1V-K2V spectral class (Pecaut and Mamajek 2013). Further support for our adopted  $T_{\rm eff1}$  value comes from the Gaia DR2 database in which the nominal  $T_{\rm eff}$  (5006 K) for this system is estimated to lie between 4761 and 5197 K (Andrae et al. 2018).

#### 3.4 Roche Modeling

#### 3.4.1 Simultaneous LC and RV solutions

The program PHOEBE 0.31a (Prša and Zwitter 2005) which features a user friendly interface to the WD2003 code (Wilson and Devinney 1971; Wilson 1979; Wilson 1990) was primarily used for initial Roche modeling of LC and RV data. Uncertainty estimates for each of the fitted parameters were ultimately derived using WDwint56a (Nelson 2009), a Windows front-end to the WD2003 source code. In both cases "Mode 3" (Wilson and Leung 1977) designated for overcontact binary systems was selected for fitting while each curve was weighted based upon observational scatter. Bolometric albedo  $(A_{1,2}=0.5)$  and gravity darkening coefficients ( $g_{1,2} = 0.32$ ) for stars with convective envelopes were respectively assigned according to Ruciński (1969) and Lucy (1967). New logarithmic limb darkening coefficients  $(x_1, x_2, y_1, y_2)$  were interpolated (Van Hamme 1993) following any change in the effective temperature for the secondary  $(T_{\text{eff2}})$  star. The effective temperature of the more massive and brighter primary constituent was fixed  $(T_{\text{eff1}} = 5140 \text{ K})$ . RV data published by Pribulla et al. (2009) were also used to further refine a LC solution for AU Ser. These data, collected in 2008, were obtained using the broadening functions extracted from the Mg I triplet region (5184 A) located within the V bandpass. As appropriate, RV data were modeled (WDwint56a) with LC data to produce the best simultaneous fits using multiple parameter subsets during DC iterations. The corresponding parameters which were varied included the center-of-mass velocity  $(V\gamma)$ , semi-major axis (SMA), mass ratio (q), surface potential  $(\Omega_1 = \Omega_2)$ , inclination (i) and  $T_{\text{eff2}}$ .

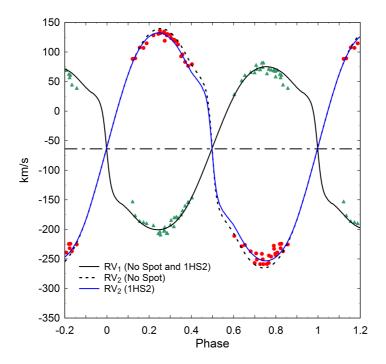
Preliminary Roche modeling attempts had revealed that the addition of a hot spot in the neck region of the secondary star was critical to successfully obtaining a good fit of the LC data. It should also be pointed out that the RV solution for the secondary (RV<sub>2</sub>) was sensitive to the absence/presence of a hot spot in the neck region (Fig. 5). This was potentially troubling since the RV data were collected in 2008 and the other multi-color LCs to be evaluated were acquired in 2011 and 2018. Fortuitously, as will be revealed in Section 3.4.3, all evaluable LCs dating from 1969 exhibit skewness about maximum light which can be simulated by the addition of a hot spot near the neck region of the secondary star. Unlike the 2011 LC in which Max I  $\sim$  Max II, sparse LC data (ASAS) collected in 2008 clearly exhibit a negative OConnell effect (O'Connell 1951) where Max II is much brighter ( $\Delta$  Max I - Max II = -0.059) than Max I (Table 4). In this regard, the

b: Interpolated Teff and spectral class range estimated from Pecaut and Mamajek (2013)

c: Median value for  $(B-V)_0=0.859\pm0.021;~T_{\rm eff1}=5140\pm125~{\rm K}$  corresponds to spectral class K1V-K2V

d: All-sky Combined Catalog of 2.5 million stars 3rd version (Kharchenko 2001)

well-sampled LC (V mag) collected in 1991 (Li et al. 1992) is the closest match ((Max I - Max II) = -0.026) to that captured during the 2008 survey. Both LCs (1991 and 2008) produced similar results ( $q = 0.684 \pm 0.006$  vs.  $0.699 \pm 0.006$ ) when simultaneously modeled with the 2008 RV data. The mean mass ratio value ( $0.692 \pm 0.006$ ) calculated from the 1991 and 2008 LCs was utilized for subsequent Roche modeling and fixed during DC iterations.



**Figure 4.** Simultaneous radial velocity (RV) solution for AU Ser without and with a single hot spot in the neck region of the secondary star (1HS2).

#### 3.4.2 Light Curves from 2011 and 2018

As mentioned previously, Roche modeling was constrained using the mass ratio ( $q = 0.692 \pm 0.006$ ) determined after simultaneously modeling RV and LC data (Section 3.4.1). This value is slightly lower than that ( $q_{\rm sp} = 0.71$ ) determined using RV data alone by Hrivnak (1993) and Pribulla et al. (2009). All other parameters except for  $T_{\rm eff1}$ ,  $A_{1,2}$  and  $g_{1,2}$  were allowed to vary during DC iterations. Multi-color parameter values and results from modeling the 2011 and 2018 LCs are found in Table 5. Corresponding unspotted (Fig. 2) simulations reveal the poor model fit during quadrature which could be significantly improved by the addition of a hot spot near the neck region shared by both stars (Fig. 3).

It is important to point out that the errors listed in Tables 5 and 6 are minimum values from the covariance matrix of the fit which assumed exact values for all fixed parameters. The incorporation of a spot to address LC asymmetry adds another layer of uncertainty due to potential degeneracy of the parameter space during Roche modeling. The shape and location of spot(s) can be highly correlated with many other parameters (e.g. inclination and surface temperature) such that the solution may not be unique.

The fill-out parameter (f) which corresponds to the degree of overcontact between each star was calculated (Eq. 2) according to Kallrath and Milone (1997):

$$f = (\Omega_{\text{inner}} - \Omega_{1,2}) / (\Omega_{\text{inner}} - \Omega_{\text{outer}}), \qquad (2)$$

where  $\Omega_{\text{outer}}$  is the outer critical Roche equipotential,  $\Omega_{\text{inner}}$  is the value for the inner critical Roche equipotential and  $\Omega_{1,2}$  denotes the common envelope surface potential for the binary system. An interesting finding (Table 6) is that the fill-out factor varies substantially (1.5 - 27.3%). One possibility considered was an association between the fill-out factor and the O'Connell effect, however, this proved not to be the case. Attempts to model the LC data from 2018 (f=4%) as a detached (Mode 2) and semi-detached (Mode 5) system never approached the best Roche lobe fits achieved when AU Ser was considered an overcontact system (Mode 3).

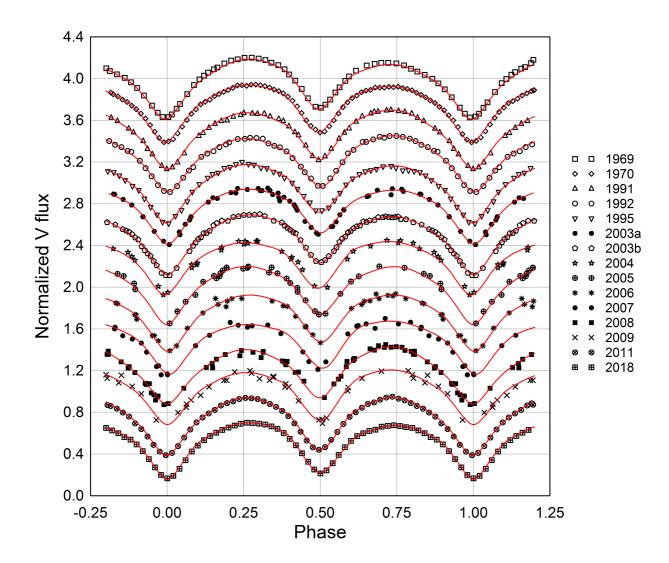


Figure 5. Folded ( $P = 0.386497 \pm 0.000001$  d) light curves for AU Ser produced from published V mag data collected between 1969 to 2009 as well as new results reported herein from 2011 and 2018. In each case, Roche modeling with the W-D code required the addition of a single hot spot in the neck region of the secondary star in order to achieve the best fits.

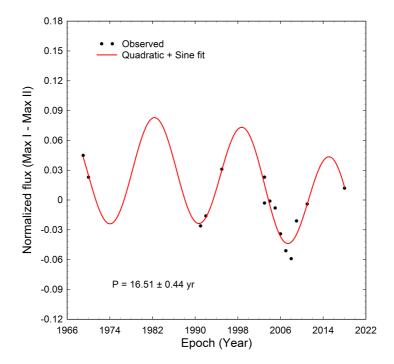


Figure 6. LC variations in Max I-Max II between 1969 and 2018. Differences were fit to a quadratic + sinusoidal expression. The results suggested that there is a  $\sim 16.5$  yr cycle that may be associated with the O'Connell effect.

**Table 4.** Differences ( $\pm$  SD) in normalized V-flux relative to Max I

Year	Max I-Min I	Max I-Min II	Max I-Max II
$1969^{1}$	0.572(6)	0.479(7)	0.045(6)
$1970^{1}$	0.561(6)	0.465(8)	0.023(6)
$1991^{2}$	0.562(8)	0.478(6)	-0.026(8)
$1992^{2}$	0.540(9)	0.484(6)	-0.016(7)
$1995^{3}$	0.544(7)	0.423(9)	0.031(4)
$2003a^{4}$	0.586(6)	0.458(4)	0.023(4)
$2003b^{5}$	0.527(9)	0.436(6)	-0.003(7)
$2004^{5}$	0.502(13)	0.463(12)	-0.001(8)
$2005^{5}$	0.564(26)	0.455(11)	-0.008(7)
$2006^{5}$	0.492(11)	0.404(11)	-0.034(8)
$2007^{5}$	0.480(10)	0.422(16)	-0.051(5)
$2008^{5}$	0.500(8)	0.425(9)	-0.059(5)
$2009^{5}$	0.447(13)	0.453(15)	-0.021(6)
$2011^{6}$	0.554(7)	0.502(6)	-0.004(8)
$2018^{6}$	0.496 (6)	0.462 (6)	0.012 (6)

<sup>(1)</sup> Binnendjik 1972; (2) Li et al. 1992; (3) Li et al. 1998; (4) Gürol 2005;

<sup>(5)</sup> ASAS survey (Pojmański et al. 2005); (6) Present study

**Table 5.** Light curve parameters employed for Roche modeling and derived geometric elements for the AU Ser light curves captured in 2011 and 2018

Parameter <sup>a</sup>	2011	2011	2018	2018
	No Spot	Spotted	No Spot	Spotted
$T_{\rm eff1}~({\rm K})^{\rm b}$	5140	5140	5140	5140
$T_{ m eff2} \ ({ m K})$	5005(3)	5006(2)	4973(2)	4986(1)
$q(m_2/m_1)$	0.692(6)	0.692(6)	0.692(6)	0.692(6)
$A^{ m b}$	0.5	0.5	0.5	0.5
$g^{ m b}$	0.32	0.32	0.32	0.32
$\Omega_1=\Omega_2$	3.106(5)	3.124(3)	3.225(3)	3.213(1)
$i^{\circ}$	84.62 (24)	83.03 (10)	83.81(24)	82.43 (10)
$A_{ m S}={ m T}_{ m S}/{ m T}$	_	1.15(1)	_	1.12(1)
$\Theta_{\rm S}$ (spot co-latitude) <sup>c</sup>	_	72.6(5)	_	90 (9)
$\phi_{\rm S}$ (spot longitude) <sup>c</sup>	_	359.8(2)	_	11.0(3)
$r_S$ (angular radius) <sup>c</sup>	_	35 (1)	_	30(2)
$L_1/(L_1+L_2)_B^{\rm d}$	0.6244(8)	0.6247(4)	0.6387(12)	0.6339(6)
$L_1/(L_1 + L_2)_V$	0.6150(5)	0.6153(2)	0.6272(3)	0.6233(1)
$L_1/(L_1 + L_2)_{I_{\rm C}}$	0.6048(5)	0.6053(2)	0.6146(3)	0.6117(1)
$r_1  ext{ (pole)}$	0.3990(2)	0.4055(8)	0.3990(2)	0.3877(4)
$r_1$ (side)	0.4242(6)	0.4321(10)	0.4242(6)	0.4094(5)
$r_1$ (back)	0.4615(9)	0.4709(14)	0.4615(9)	0.4392(7)
$r_2$ (pole)	0.3447(5)	0.3444(8)	0.3447(5)	0.3264(4)
$r_2$ (side)	0.3634(6)	0.3636(10)	0.3634(6)	0.3416(5)
$r_2$ (back)	0.4053(10)	0.4083(16)	0.4053(10)	0.3739(7)
Fill-out factor (%)	30.5	25.9	1.1	4.0
$rms (B)^e$	0.04611	0.02499	0.03430	0.01821
$\operatorname{rms}(V)^{\operatorname{e}}$	0.02646	0.01478	0.02281	0.01228
$ m rms~(I_C)^e$	0.02034	0.01314	0.01530	0.00976

a: All error estimates for  $T_{\rm eff2},~q,~\Omega_{1,2},~A_S,~\Theta_{\rm S},~\phi_{\rm S},~r_{\rm S},~r_{1,2},~L_1$  from WDwint56a (Nelson 2009)

b: Fixed during DC

 $<sup>\</sup>ensuremath{\mathbf{c}}\xspace$  Secondary spot temperature, location and size parameters in degrees

d: Bandpass dependent fractional luminosity;  $L_1$  and  $L_2$  refer to scaled luminosities of the primary (more massive) and secondary stars, respectively

e: Root mean square error of model fit

#### 3.4.3 Retrospective analysis of LCs from 1969-2009

W-D modeling (V mag) of the six previously published LCs (Binnendjik 1972; Li et al. 1992; Li et al. 1998; Gürol 2005) was performed with and without a hot spot located near the neck region in a manner similar to that previously described for the 2011 and 2018 data. In addition, sparsely sampled ASAS survey data (V mag) collected between 2003 and 2009 (Pojmański et al. 2005) were phased to produce yearly LCs (Fig. 6) using the ANOVA routine (Schwarzenberg-Czerny 1996) in Peranso 2.5 (Paunzen and Vanmunster 2016). Only the spotted solutions from this retrospective analysis are included herein. Roche modeling of the LCs generated during this period of time provided additional information to chronicle the behavior of AU Ser over a longer period of time than was available to Gürol (2005). Relative V-flux levels at Min I, Min II, Max I and Max II were estimated using polynomial fits near each LC region of interest. A positive OConnell effect (Max I > Max II) was observed in 1969, 1970, 1995, 2003a and 2018, whereas Max II >Max I in 1991, 1992, and between 2005-2009. LCs from 2003b, 2004 and 2011 did not exhibit any meaningful ( $\leq 0.004$ ) differences in maximum light (Table 4). It should be noted that photometric data captured by Gürol (2005) in 2003 occurred between 22 July and 26 Aug 2003, whereas the majority (80%) of the data during the ASAS survey were acquired before 22 July 2003. This may explain differences in the modeling results (2003a vs. 2003b).

A quadratic + sinusoidal fit (Fig. 7) of flux normalized Max I - Max II values over time (1969-2011) uncovered a periodic change (16.51  $\pm$  0.44 yr) in the LCs. Gürol (2005) performed a similar analysis but over a shorter time frame (1969-2003) and arrived at a different conclusion which suggested the most probable period for flux variation relative to Max I ranged between 32 and 35 yr. Upon further examination, one finds that Gürol (2005) proposed two other possible solutions at 8.9 and 17.3 yr. It is not hard to imagine period harmonics which are simple multiples in the ratio 8.5:17:34. The middle value closely approximates the more robust period estimate from this study and indicates that flux change relative to that observed at Max I occurred nearly every 17 yr and corresponds to the transition from a positive to negative O'Connell effect. Furthermore, assessment of the LCs and each corresponding Roche model fit (Table 6) offer compelling evidence for persistent feature(s) on AU Ser that skew maximum light to occur after  $\phi = 0.25$  and then before  $\phi = 0.75$ ; the best fits were consistently achieved by positioning a hot spot on or near the neck region of the secondary star.

As depicted in Figure 8, spatial models of AU Ser showing the sequence of hot spot locations were rendered with BM3 using the physical and geometric elements determined from all LCs investigated herein. As might be expected, the longitudinal position of the hot spot relative to the neck center (0°) is highly correlated (r=0.913) with the difference between Max I and Max II (Fig. 9). A working hypothesis posits the transfer of mass from the primary to the secondary; the net effect is a tightening of the orbital radius and as is observed (Section 3.6), a decrease in orbital period. The transfer of matter and energy onto the secondary is mediated through the neck region and may result in the formation of a hot spot (Maceroni and van't Veer 1993). Not surprisingly when comparing the multi-color LCs from 2011 and 2018, increased brightness and skewed timings during maximum light were observed in the more energetic region (B bandpass) of the visual spectrum. Although not uncommon for overcontact binaries, X-ray emission coincident with the position for AU Ser was detected by Szczygieł et al. (2008) using a combined database generated from the ASAS and ROSAT All Sky Survey. In this case, it is not known whether X-ray emission corresponds to changes in orbital phase when a putative

hot spot would be maximally exposed.

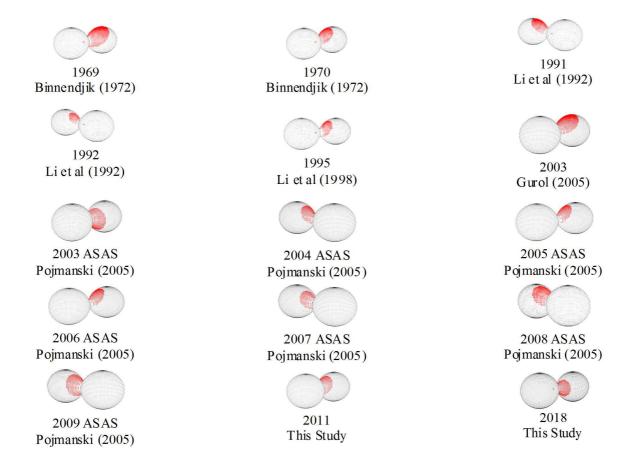


Figure 7. AU Ser spatial models rendered with BM3 showing movement of the hot spot on or near the neck region of the secondary star between 1969-2018

Table 6. Light curve (V mag) parameters employed for Roche modeling (spotted) and derived geometric elements from AU Ser light curves captured between 1969 and 2018.

Parameter	$1969^{1}$	$1970^{1}$	$1991^{2}$	$1992^{2}$	$1995^{3}$	$2003a^{4}$	$2003b^{5}$	$2004^{5}$	$2005^{5}$	$2006^{5}$	$2007^{5}$	$2008^{5}$	$2009^{5}$	$2011^{6}$	$2018^{6}$
$T_{\rm eff1}~({\rm K})^{\rm b}$	5140	5140	5140	5140	5140	5140	5140	5140	5140	5140	5140	5140	5140	5140	5140
$T_{\rm eff1}$ (K)	4907(3)	4896(2)	4942(4)	4991(5)	4875(6)	4863(4)	4896(7)	4969(9)	4882(11)	4916(12)	4954(12)	4998(24)	5054(13)	5014(1)	4986(1)
$q(m_2/m_1)$	0.692(6)	0.692(6)	0.684(6)	0.692(6)	0.692(6)	0.692(6)	0.692(6)	0.692(6)	0.692(6)	0.692(6)	0.692(6)	0.699(6)	0.692(6)	0.692(6)	0.692(6)
$A^{b}$	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5
$g^{\mathrm{b}}$	0.32	0.32	0.32	0.32	0.32	0.32	0.32	0.32	0.32	0.32	0.32	0.32	0.32	0.32	0.32
$\Omega_{1,2}$	3.18(1)	3.19(1)	3.12(1)	3.16(1)	3.16(1)	3.18(1)	3.23(1)	3.22(1)	3.17(2)	3.19(2)	3.21(2)	3.19(2)	3.19(3)	3.13(3)	3.21(1)
$i^{\circ}$	82.1(2)	82.0(1)	82.2(1)	81.5(3)	83.0(4)	83.2(2)	82.0(4)	81.0(1)	82.3(7)	81.2(8)	81.3(7)	82.7(1.8)	80.2(1.1)	82.8(1)	82.4(1)
$A_S = T_S/T$	1.11(1)	1.16(1)	1.17(1)	1.19(1)	1.11(1)	1.13(1)	1.14(1)	1.11(1)	1.11(1)	1.14(1)	1.15(2)	1.12(1)	1.12(1)	1.14(1)	1.12(1)
$\Theta_{\rm S}$ (co-lat.) <sup>c</sup>	49.6 (1.3)	59.6(1.3)	50(12)	65 (3)	70 (7)	46.2(2)	19.6(1)	70 (4)	65(15)	62(5)	56 (18)	59 (12)	79.5(7.3)	71.1(1)	90 (1)
$\phi_{\rm S} \ ({\rm long.})^{\rm c}$	18.5 (1.1)	4.2(4)	352(3)	350 (1)	5(2)	6 (1)	6(2)	355 (4)	2(5)	0 (3)	345 (5)	350 (6)	350 (6)	0(1)	11 (1)
$r_S$ (radius) <sup>c</sup>	60.1(6)	37.3(2)	40 (1)	25(1)	35(1)	48 (1)	48 (1)	33.8(1.6)	34 (3)	35 (8)	28(3)	36(2)	36(2)	35(1)	30(1)
Fill-out (%)	12.9	10.4	24.4	15	17	13	5.3	1.5	13.7	10.4	10.0	27.3	5.8	25.7	4

<sup>1.</sup> Binnendijk 1970; 2. Li et al. 1992; 3. Li et al. 1998; 4. Gürol 2005; 5. Pojmański et al. 2005; 6. This study a: All error estimates for  $T_{eff2}, q, \Omega_{1,2}, A_S, \Theta_S, \phi_S, r_S$  from WDwint56a (Nelson 2009) b: Values fixed during DC c: Positional ( $\Theta$  and  $\phi$ ) and size ( $r_S$ ) spot parameters in degrees

**Table 7.** Mean absolute parameters ( $\pm$ SD) for AU Ser using results from the

ultaneous (L	C and RV) Roch	ne model fit of $V$	mag data from	n 1991	and
	Parameter	Primary	Secondary	_	
•	$M_{ass}(M_{\odot})$	0.85(3)	0.59 (2)		

Parameter	Primary	Secondary
Mass $(M_{\odot})$	0.85(3)	0.59(2)
Radius $(R_{\odot})$	1.04(1)	0.88(1)
$a~(R_{\odot})$	2.52(3)	_
Luminosity $(L_{\odot})$	0.675(13)	0.427(9)
$M_{ m bol}$	5.177(22)	5.675(22)
$\log(g)$	4.336(16)	4.323(16)

#### 3.5 Absolute Parameters

Absolute parameters (Table 7) were derived for each star in this A-type W UMa binary system using results from the best fit spotted model simulations from 1991 and 2008. Aside from a spectroscopic mass ratio  $(q_{\rm sp})$ , another critical piece of information supplied by an RV experiment is the determination of the orbital speeds  $(v_{\rm 1r} + v_{\rm 2r})$  whereby the total mass can be readily calculated according to Eq. 3 when the orbital inclination is also known:

$$(m_1 + m_2)\sin^3 i = (P/2\pi G)(v_{1r} + v_{2r})^3.$$
(3)

In this case from the mean simultaneous fit of LC and RV data (1991 and 2008),  $K_1 = 135.2 \pm 1.1 \,\mathrm{km/s}$ ,  $K_2 = 195.5 \pm 1.8 \,\mathrm{km/s}$ ,  $V_{\gamma} = -63.8 \pm 0.68 \,\mathrm{km/s}$  and  $i = 82.5 \pm 1.8^{\circ}$ . The total mass of the system was determined to be  $1.44 \pm 0.05 \,M_{\odot}$  so it follows that since  $q = 0.692 \pm 0.006$  then the primary mass  $= 0.85 \pm 0.03 \,M_{\odot}$  and secondary mass  $= 0.59 \pm 0.02 \,M_{\odot}$ .

The semi-major axis,  $a(R_{\odot}) = 2.52\pm0.03$ , was calculated according to Newton's version (Eq. 4) of Keplers third law where:

$$a^3 = G \times P^2(M_1 + M_2)/4\pi^2. \tag{4}$$

The effective radii of each Roche lobe  $(R_L)$  can be calculated to within an error of 1% over the entire range of mass ratios  $(0 < q < \infty)$  according to the expression (5) derived by Eggleton (1983):

$$r_L = (0.49q^{(2/3)})/(0.6q^{(2/3)} + \ln(1 + q^{(1/3)}))$$
(5)

from which values for  $r_1$  (0.4112  $\pm$  0.0005) and  $r_2$  (0.3475  $\pm$  0.0005) were respectively determined for the primary and secondary stars. Since the semi-major axis and the volume radii are known, one can calculate the solar radii for both binary constituents where  $R_1$  = a  $\times$   $r_1$  = 1.04  $\pm$  0.01  $R_{\odot}$  and  $R_2$  = a  $\times$   $r_2$  = 0.88  $\pm$  0.01  $R_{\odot}$ .

The bolometric magnitudes (Mbol<sub>1,2</sub>) and luminosity in solar units ( $L_{\odot}$ ) for the primary ( $L_{1}$ ) and secondary stars ( $L_{2}$ ) were calculated from well known relationships for bolometric magnitude (Eq. 6) and luminosity (Eq. 7) where:

$$M_{bol1,2} = 4.75 - 5\log(R_{1,2}/R_{\odot}) - 10\log(T_{1,2}/T_{\odot})$$
 (6)

and

$$L_{1,2} = (R_{1,2}/R_{\odot})^2 (T_{1,2}/T_{\odot})^4.$$
 (7)

Pooling the results for  $T_{eff2}$  across all LCs (1991-2018) leads to a mean value of 4943  $\pm$  58 K (Table 6). Assuming that  $T_{\rm eff1} = 5140$  K and  $T_{\odot} = 5778$  K, then  $L_{\odot}$  for the primary

and secondary are  $0.675 \pm 0.013$  and  $0.427 \pm 0.020$ , respectively. Bolometric magnitudes were calculated to be  $M_{\rm bol1} = 5.127 \pm 0.009$  and  $M_{\rm bol2} = 5.691 \pm 0.052$ . Combining the bolometric magnitudes resulted in an absolute value ( $M_V = 4.663 \pm 0.009$ ) when adjusted with the bolometric correction (BC= -0.272) interpolated from Pecaut and Mamajek (2013). Substituting into the Eq. 8, the distance modulus:

$$d(pc) = 10^{((m-M_V)-A_V+5)/5)}, (8)$$

where  $m = V_{\text{avg}}(10.71 \pm 0.01)$  and  $A_V = 0.065$  leads to an estimated distance of  $171 \pm 2$  pc to AU Ser which is 5% higher than that  $(164 \pm 1 \text{ pc})$  calculated directly from parallax data recently included in the Gaia DR2 release (Brown et al. 2018). Although not unreasonable, this discrepancy may result from the use of MPOSC3-catalog based magnitudes rather than determining values from absolute photometry with reference star field standards.

#### 3.6 Period analyses from eclipse time differences

Over the years there have been many period studies of this system. Kennedy (1985) was the first to suggest that changes had occurred in the eclipse timing differences (ETDs) for AU Ser. Qian et al. (1999) performed the first systematic examination of period and light time variations for this system and noted that the orbital period suddenly decreased between 1987 and 1988. They suggested there might be a connection between the light curve asymmetries and sudden changes in the orbital period. The next detailed analysis of the ETDs was conducted by Gürol (2005) in which he modeled the residuals over time with a quadratic plus sinusoidal equation and subsequently dismissed the notion of a sudden period change. Furthermore Gürol (2005) proposed that the predominant cyclic behavior with a period of about 94 yr was most likely associated with the light-time-effect (LiTE) caused by an invisible but gravitationally bound third star.

A case, albeit somewhat less convincing, can be made which argues against the presence of a gravitationally-bound third body. It should be noted that during our Roche modeling,  $l_3$ , the third light parameter, was not significantly different from zero when allowed to freely vary during iterative DC. This implies that a putative gravitational partner in this system is either too small to detect during simulations of the observed light curve data or that some other phenomena are responsible for the  $\sim 94$  yr periodicity in the eclipse timing residuals. Assuming that the putative third body is still on the main sequence its absolute luminosity can be estimated according to the mass-luminosity relationship where  $L \sim M^{3.5}$ . The fractional luminosity of the third constituent  $(L_3)$  can be calculated from the expression (Eq. 9):

$$L_3(\%) = (100 \times M_{3,\min}^{3.5}) / (L_1 + L_2 + M_{3,\min}^{3.5})$$
(9)

where  $M_3$  is the minimum mass determined when  $i = 90^{\circ}$  and  $L_1$  and  $L_2$  are the luminosities in solar units  $(L_{\odot})$  determined for the primary and secondary stars (Table 7).

Comparisons among third body solutions proposed by Gürol (2005), Amin (2015), Nelson et al. (2016) and this study are summarized in Table 8. According to our LiTE modeling, the luminosity contributed by a third body ( $L_3 \sim 1.2\%$ ) where  $M_3 = 0.293~M_{\odot}$  would be challenging to detect photometrically. However, the minimum mass estimates for a third body reported (Table 8) by Amin (2015) and Gürol (2005) would have resulted in even greater contributions ( $L_3 > 6\%$ ) to the total luminosity of the system. According to their LiTE modeling results, this extra light (l) should have been detected during W-D modeling of LC data. Finally, another confounding result arguing against LiTE comes

from an RV study in which Pribulla et al. (2009) did not see spectroscopic evidence for a third body in the broadening functions. It is clear that additional high-precision photometric and spectroscopic data will be necessary to fully tease out the effect(s) which lead to episodic changes in the eclipse timings for AU Ser.

Amin (2015) and Nelson et al. (2016) re-examined the period behavior of AU Ser using ETD data gathered between 1936 and 2015. Modeling efforts by Amin (2015) which included 39 new minima times led to values for a putative third body which contrast sharply with the period ( $P_3$ ) and semi-amplitude (A) reported by Gürol (2005) and Nelson et al. (2016). There was, however, general concurrence between Amin (2015) and Gürol (2005) that the mechanism for a light-time effect was probably not due to cycles in magnetic activity attributed to Applegate (1992). This is further supported using an empirical relationship (Eq. 10) between the length of orbital period modulation and angular velocity ( $\omega = 2\pi/P_{\rm orb}$ ) that was developed by Lanza and Rodonò (1999):

$$\log P_{\text{mod}}[y] = 0.018 - 0.36 \times \log (2\pi (P_{\text{orb}}[s])). \tag{10}$$

In this case any period modulation resulting from a change in the gravitational quadrupole moment would probably be closer to 23 yr for AU Ser, not the longer periods ( $P_3$ ) 42 yr) proposed by Gürol (2005) and Amin (2015). Significant differences in the quadratic coefficient were reported depending upon whether or not visual (vis) and photographic (pg) data were included in the analyses. This disparity points out the vagaries associated with period change and mass transfer analysis from eclipse timing residuals; other factors contributing to error are discussed in depth in a series of papers by Nelson et al. (2014; 2015; 2016). Ironically in Nelson et al. (2016), several widely different LiTE solutions emerged:  $A_1$  (an update to the analysis of Gürol (2005) but using LiTE analysis in which  $P_3 = 29.9 \text{ yr}$ ),  $B_1$  (another update to Gürol 2005 where  $P_3 = 96.4 \text{ yr}$ ), and finally a new fit, solution C ( $P_3 = 38.6 \text{ yr}$ ). Nelson et al. (2016) concluded that it was "problematic which solution to choose"; however they favored solution  $A_1$ . Here again it was evident with our fresh analysis which includes ETs reported by Gürol (2005) and Amin (2015) and 10 new ETs from this study, that many early pg and vis eclipse timings identified as outliers in Fig. 10 seemingly describe a completely different pattern than all the others derived from ccd and photoelectric (pe) analyses. Removal of these data from consideration was not taken lightly, however, as it became very clear after multiple model iterations, their inclusion made it impossible to properly simulate the orbital period variability of AU Ser after 1969. This would severely limit the ability to predict future behavior of AU Ser and thus derive a robust hypothesis for the underlying sinusoidal-like variations in the orbital period. Data included in all subsequent (1969-2018) curve fitting were weighted in the ratio 0.04:1:1 (vis:pe:ccd).

Stepping back for a moment to first principles, shifts in the times of minimum light under the influence of a third body orbiting a binary system can be evaluated according to the generalized expression (Eq. 11):

$$(ETD)_{fitted} = c_0 + c_1 E + c_2 E^2 + \tau,$$
 (11)

where  $c_0$ ,  $c_1$  and  $c_2$  are constants, E = cycle or epoch number, and  $\tau = \text{time}$  difference due to orbital motion, an expression derived by Irwin (1952; 1959). Ignoring the last term ( $\tau$ =0) for the moment, initial curve fitting (scaled Levenberg-Marquardt algorithm) revealed a quadratic coefficient ( $c_2 \approx -5.0 \times 10^{-11}$ ) that is less than zero (downwardly turned parabola) suggesting that the orbital period is decreasing at a constant rate. A secular change defined by a parabola is often attributed to mass transfer or by angular

momentum loss (AML) due to magnetic stellar wind. Ideally when AML dominates the net effect is a decreasing orbital period whereas the opposite is observed with conservative mass transfer from the secondary to the primary star. Notably, residuals from the quadratic model fit also describe an underlying sinusoidal-like variation in the orbital period. As long as this sinusoidal curve appears symmetrical as suggested in the middle panel of Fig. 10, this behavior can be fit in its simplest form using a quadratic formula (Eq. 12) modulated with a sine term  $(\tau)$  such that:

$$(ETD)_{\text{fitted}} = c_0 + c_1 E + c_2 E^2 + c_3 \sin(c_4 E + c_5)$$
(12)

where  $c_0$ ,  $c_1$  and  $c_2$  are constants, E = cycle number, and  $\tau = \text{time}$  difference due to orbital motion. This simplified light-time effect (LiTE) analysis using a scaled Levenberg-Marquardt (L-M) algorithm assumes that the putative third body revolves about a common gravitational center in a circular orbit (e=0). The amplitude of the oscillation, as defined by the coefficient of the sine term ( $c_3$ ), was determined to be 0.0116  $\pm$  0.0003 d while the period of the sinusoidal oscillations was calculated ( $P_3 = 31.2 \pm 0.3 \text{ yr}$ ) according to the expression (Eq. 13):

$$P_3 = 2\pi P/\omega \,, \tag{13}$$

where  $\omega$ , the angular frequency, is defined by the coefficient  $c_4$  (0.000213  $\pm$  0.000004) and P is the orbital period of the binary pair in days. Cyclic changes of eclipse timings may result from the gravitational influence of unseen companion(s) and/or periodic changes in the magnetic activity of either binary constituent. It has been well documented that a significant percentage (> 50%) of overcontact binaries exist as multiple systems (Pribulla et al. 2006; D'Angelo et al. 2006). Additional analyses including the associated parameters in the LiTE equation (Irwin 1952; 1959) were derived using the Solver routine in an Excel spreadsheet described by Nelson et al. (2016). These parameters include:  $P_3$  (orbital period of star 3 and the 1-2 pair about their common center of mass), e (orbital eccentricity),  $\omega$  (argument of periastron),  $t_3$  (time of periastron passage) and the semi-amplitude (A) of the light-time effect. The semi-amplitude is further defined as  $A = a_{12}\sin(i_3) \times c^{-1}$ where  $a_{12}=$  semi-major axis of the 1-2 pair's orbit about the center of mass of the 3-star system,  $i_3$  = orbital inclination of the 3-star system, and c = speed of light. These five parameters, as well as the coefficients  $c_0$ ,  $c_1$ , and  $c_2$  from Eq. 12 add up to a total of eight variables which are factored into LiTE modeling. It was apparent from our simplified L-M solution  $(P_3 = 31.2 \pm 0.3 \text{ yr})$  which included 10 new times-of-minima (Table 8) that period  $(P_3)$  solutions  $A_1$  (29.8 yr) and  $A_2$  (29.4 yr) from Nelson et al. (2016) were very close. We repeated this simplest solution which fixes the third body with a circular orbit (e=0) and another where e is allowed to vary using the aforementioned eight parameter Excel Solver routine to optimize the LiTE fit. These two analyses produced similar results when comparing the root mean square errors (Table 8). The latter solution in which a putative third body revolves in a somewhat eccentric orbit (e = 0.168) appears to offer a slightly improved fit but at the expense of an increased error estimate for  $P_3$  (31.36  $\pm$  1.18 vs.  $31.49 \pm 0.40$  yr). Nonetheless, considering an improbably stable circular orbit for a circumbinary star, we arrive at a preferred solution in which the orbit is slightly elliptical  $(e = 0.168 \pm 0.023)$ . Thereafter it was possible to subtract out the LiTE component of the ETD values leaving, in this case, a parabolic relationship with quadratic constant  $c_2 = -6.19(20) \times 10^{-11}$  d (Fig. 10). Assuming that the secular decrease in orbital period is associated with mass loss from the primary to the secondary, then a period rate loss  $(dP/dt = -1.17(4) \times 10^{-7} \text{ d/yr})$  can be estimated from Eq. 14:

$$dP/dt = 2 \times (365.24) \times c_2/P.$$
 (14)

Parameter	Units	Gürol (2005)	Amin (2015)	Nelson et al.	This study	This study
	0 0.0	0.4222	()	(2016)		
$t_0$	$\mathrm{HJD^a}$	44722.4515	44722.4683 (14)	44722.4472	44722.4725	44722.4725
$t_3$ (init, epoch)	[d]	10023.9468		10857 (533)	_	10176 (2666)
$P_3$ (period)	[yr]	94.15	43 (3)	29.8(5)	31.49(40)	31.36 (1.18)
A (Amplitude)	[d]	0.0355	0.0197(16)	0.0110(3)	0.0109(2)	0.0116(4)
e (eccentricity)		0.48	0.52(12)	0	0	0.168(23)
$\omega$ , arg. periast.	0	147.7	_	_	_	163.7 (20.5)
$a_{12}\sin(i)$	[AU]	_	3.66(30)	1.90(5)	1.89(3)	2.01 (8)
$f(m_3)$	${ m M}_{\odot}$	0.034199	0.02662(13)	0.0077(5)	0.0068(4)	0.0082(14)
$M_3 \ (i=90^{\circ})$	${ m M}_{\odot}$	0.53	0.475(1)	_	0.271	0.293
$M_3 \ (i=60^{\circ})$	${ m M}_{\odot}$	_	0.564(1)	_	0.319	0.342
$M_3 \ (i=30^{\circ})$	${ m M}_{\odot}$	_	1.153(3)	_	0.612	0.661
$c_2$ (Quad. coeff.)	$\times 10^{-11}$	-7.29	-4.69	-6.8(3)	-6.28(8)	-6.19(20)
dP/dt	$10^{-7} {\rm d/yr}$	-1.378	-0.887		-1.19(1)	-1.17(4)
$dM_1/dt$	$10^{-7} M_{\odot} / {\rm yr}$	-2.598	_	_	-1.95(8)	-1.93(10)
$\mathrm{rss}^{\mathrm{b}}$					0.000643433	0.000612608

**Table 8.** Putative period change, mass loss and third-body solution to the light-time effect observed from changes in AU Ser eclipse timings

Finally, the rate of conservative mass transfer was calculated using Eq. 15:

$$dM/dt = M_1 M_2 / (3P(M_1 - M_2))dP/dt, (15)$$

where  $M_1$  is the mass of the primary star in solar units,  $M_2$  is the mass of the secondary star in solar units, and P is the orbital period of binary pair. Accordingly, the mass-transfer rate  $(dM_1/dt)$  for AU Ser was estimated to be  $-1.93(10) \times 10^{-7} M_{\odot}/\text{yr}$ .

# 4 Conclusions

Reported herein are the first  $BVI_{\rm C}$  CCD-based light curves for AU Ser which have also produced 10 new times of minimum for this A-type W UMa binary system. Evidence from this study and other surveys suggested that the effective temperature of the primary star was  $\sim 5140$  K which corresponds to a spectral class range between K1V and K2V. During Roche modeling with the W-D code, a spotted solution was necessary since all evaluable LCs from 1969 to 2018 exhibited asymmetry with regard to intensity and/or peak skewness during quadrature (maximum light was displaced after  $\phi = 0.25$  and before  $\phi = 0.75$ ). Positioning a single hot spot on the secondary near the neck between both stars produced the best Roche model fits. The relative location of the secondary hot spot corresponded to cyclical changes ( $\sim 16.5 \text{ yr}$ ) which appeared to be associated with the so-called "O'Connell effect". Regression analyses performed using ETDs indicate that the orbital period for AU Ser has been decreasing at a rate of  $\sim 1.18 \times 10^{-7} \text{ d yr}^{-1}$ . This secular change in orbital period may be related to mass transfer from the primary onto the secondary and is consistent with the appearance of a persistent hot spot in the neck region of the secondary star. LiTE analysis on a subset of time-of-minimum observations spanning the last 49 years uncovered a sinusoidal-like variation  $(P_3 \sim 31.36 \text{ yr})$  in the orbital period of the binary pair. This was most likely associated with the gravitational influence of a third body, however, the possibility of other forces at play (eg. cycles in

a: HJD-24000000

b: Residual Sum of Squares (rss)

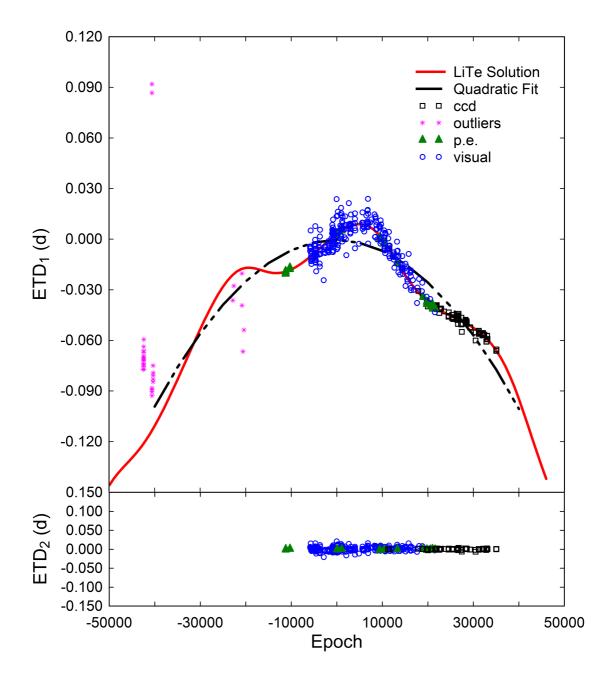


Figure 8. Preferred LiTE solution ( $P_3 = 31.36 \pm 1.2$  yr) incorporating 10 new eclipse timings for AU Ser. The top panel includes all eclipse time differences (ETD<sub>1</sub>) however the model fit does not include those labeled as "Outliers = \*". The bottom panel shows the residuals (ETD<sub>2</sub>) remaining from the final LiTE fit.

magnetic activity) cannot be completely discounted. As is often the case with complex behaviors uncovered by analyzing secular changes in overcontact binary systems, many more years of data will likely be required to confirm the true nature of periodic variation observed in the eclipse timings.

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